

# **Gas Density/Pressure Enhanced Regions as Favorable Places for the Formation of Planetesimals via Gravitational Instability**

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Development of Prebiotic Conditions

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# Pressure-Enhanced Regions

Pressure/density structures can appear in a disk due to

**1) the radial out-flow of gas molecules due to the inward radial migration of solids due to the gas drag**

(Korbet et al. 2001)

**2) the appearance of vortices**

(Barge & Sommeria 1995, Bracco et al. 1998, Klahr & Bodenheimer 2003)

**3) clumps**

(Boss 2001, Mayer et al. 2004, Rice et al. 2004, Durisen et al. 2005)

**4) interaction of the disk with a stellar companion**

(Mayer et al. 2005, Boss 2006)

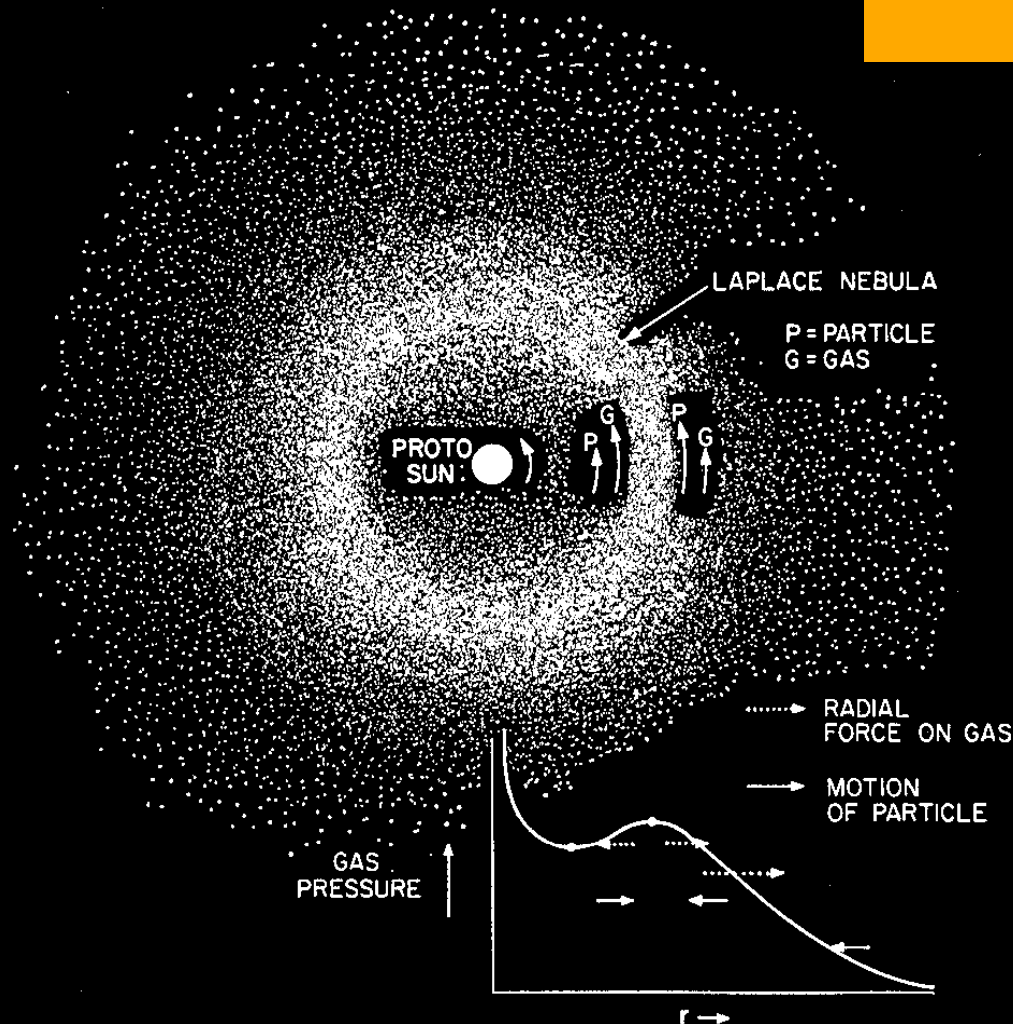
Gas angular frequency

$$r\omega_g^2 = r\omega_K^2 + \frac{1}{\rho_g(\vec{R})} \frac{\partial P_g(\vec{R})}{\partial r}$$

Gas Pressure

Keplerian frequency

Gas density



Objects outside the maximum pressure feel a headwind and spiral toward the star, whereas objects inside feel a tailwind and spiral out.

# A Heuristic Model

(Haghighipour & Boss 2003)

$$\rho_g(r,z) = \rho_g(r,0) \exp\left\{\frac{GMm_0}{K_B T} \left[ \frac{1}{(r^2 + z^2)^{1/2}} - \frac{1}{r} \right]\right\}$$

$$\rho_g(r,0) = \rho_0 \exp\left[-\beta \left(\frac{r}{r_m} - 1\right)^2\right]$$

Gas : Molecular Hydrogen

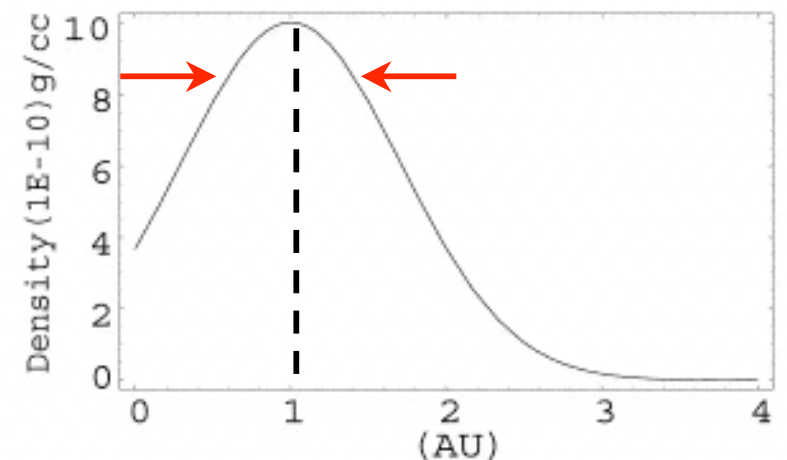
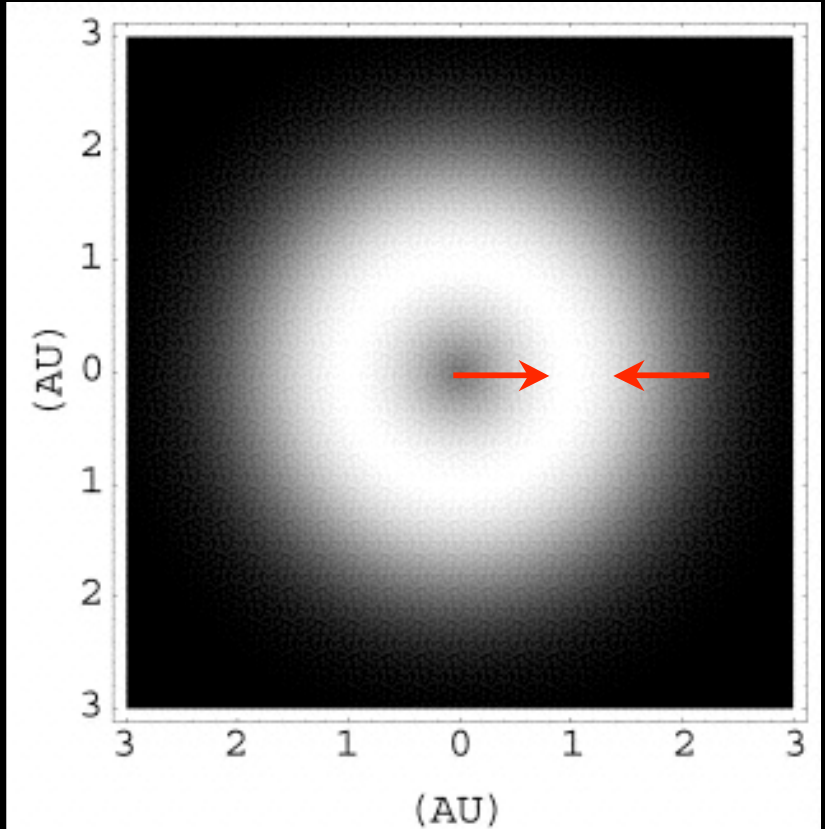
Star : Sun

$T = 100 \text{ K}$

$\rho_0 = 10^{-9} \text{ g/cm}^3$

$\beta = 1$

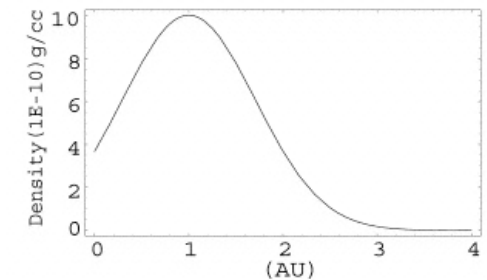
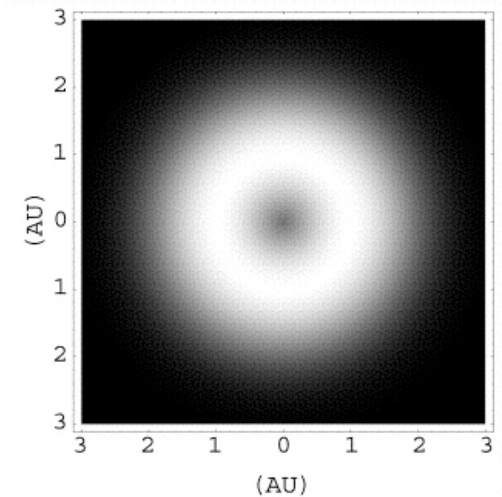
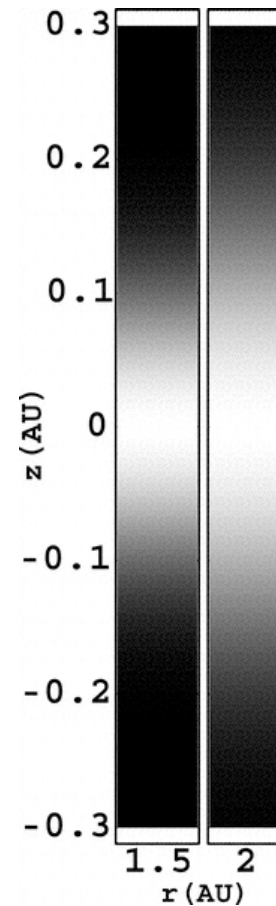
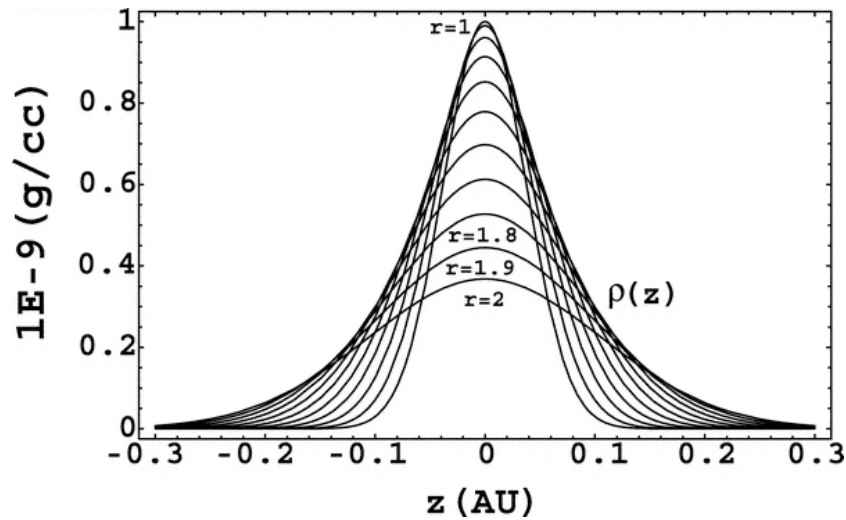
$r_m = 1 \text{ AU}$



# A Heuristic Model

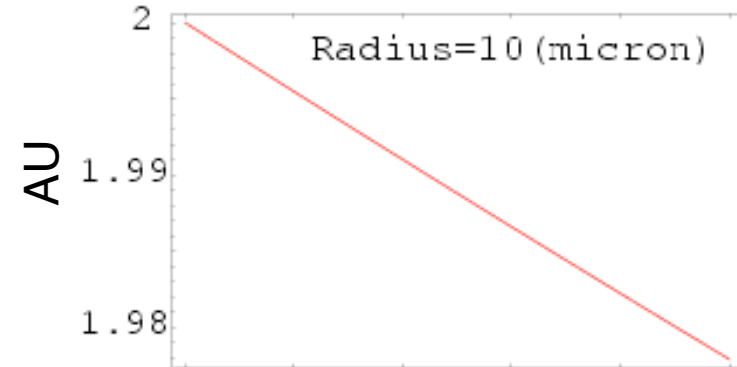
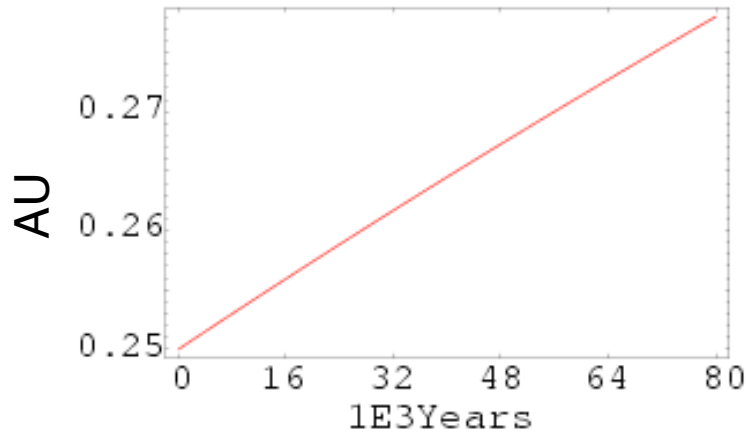
$$\rho_g(r,z) = \rho_0 \text{Exp} \left\{ \frac{8GM}{\pi \bar{v}_{\text{th}}} \left[ \frac{1}{(r^2 + z^2)^{1/2}} - \frac{1}{r} \right] - \beta \left( \frac{r}{r_m} - 1 \right)^2 \right\}$$

$$\rho_{\text{dust}} = 0.0034 \rho_g$$

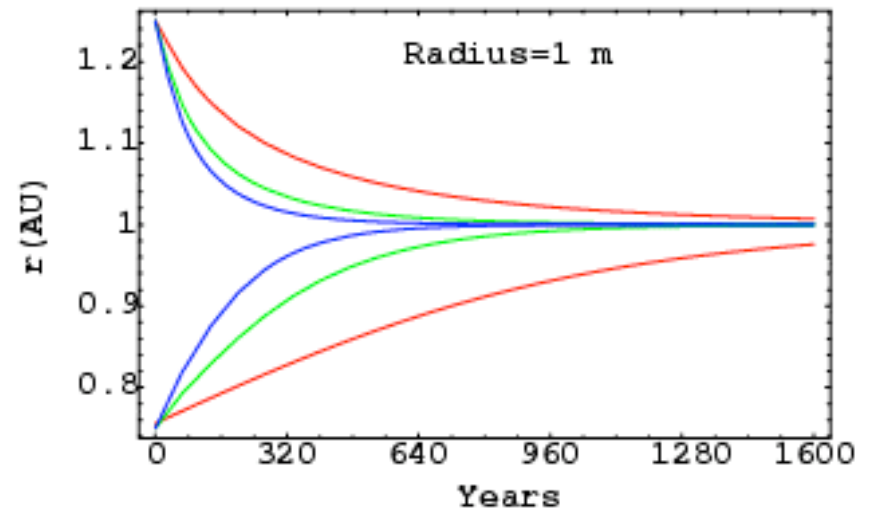
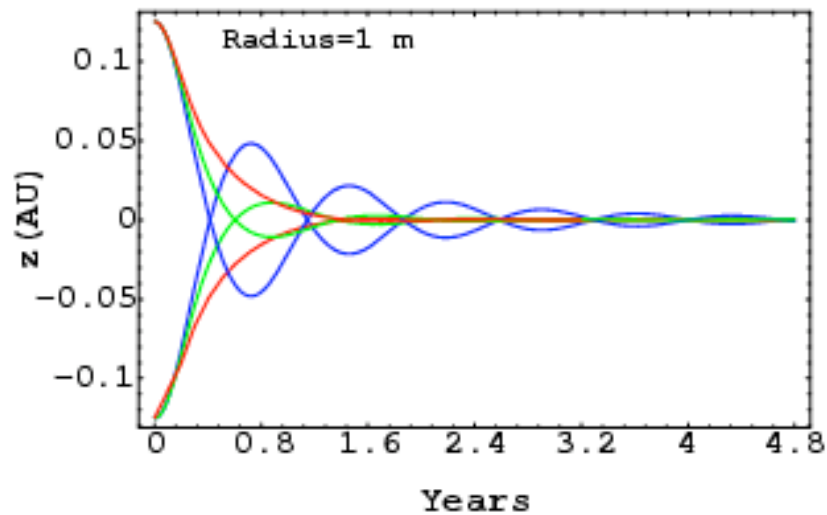


# Radial migration of a dust particle

(Haghighipour & Boss, 2003a)



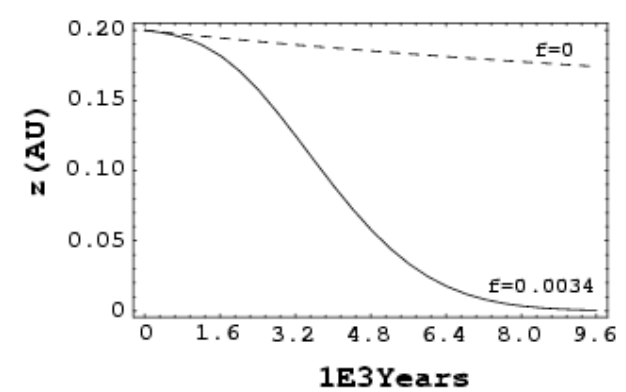
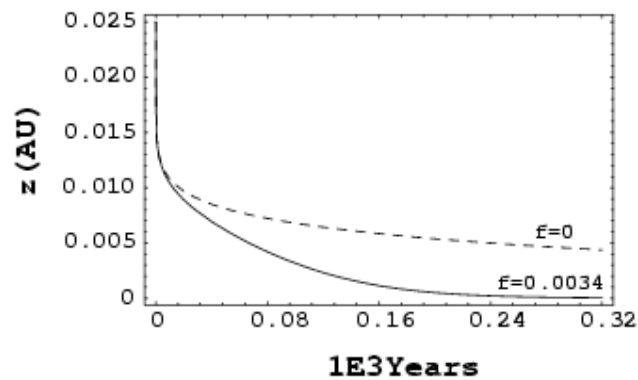
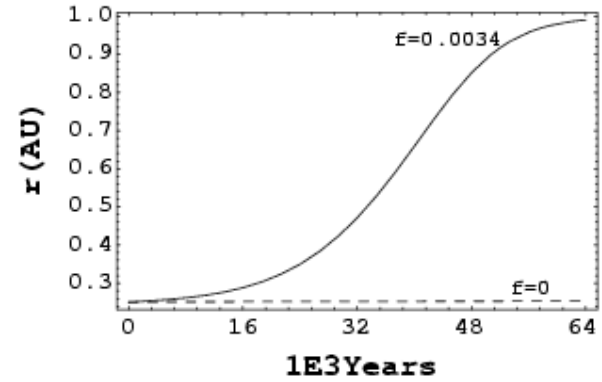
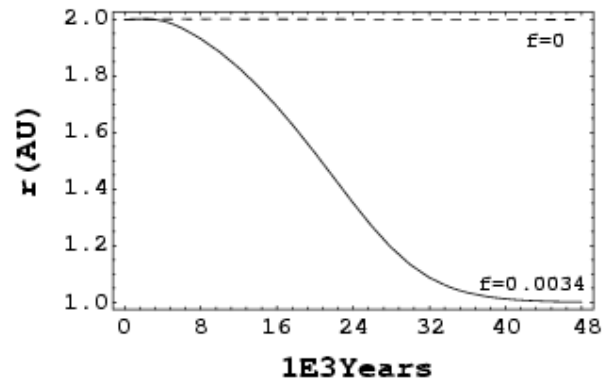
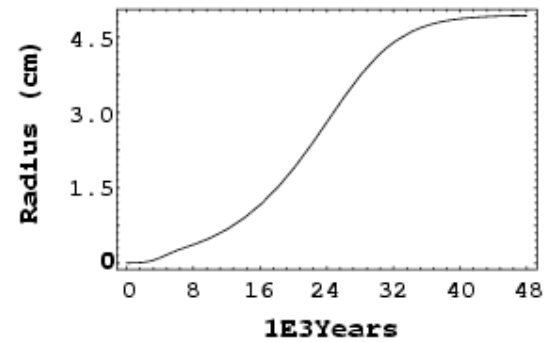
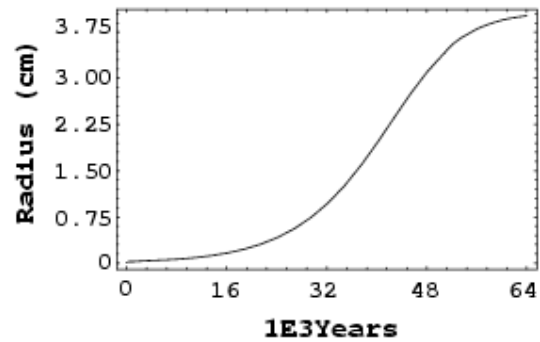
## Vertical(left) and radial (right) migration of a meter-size object



(Haghighipour & Boss, 2003b)

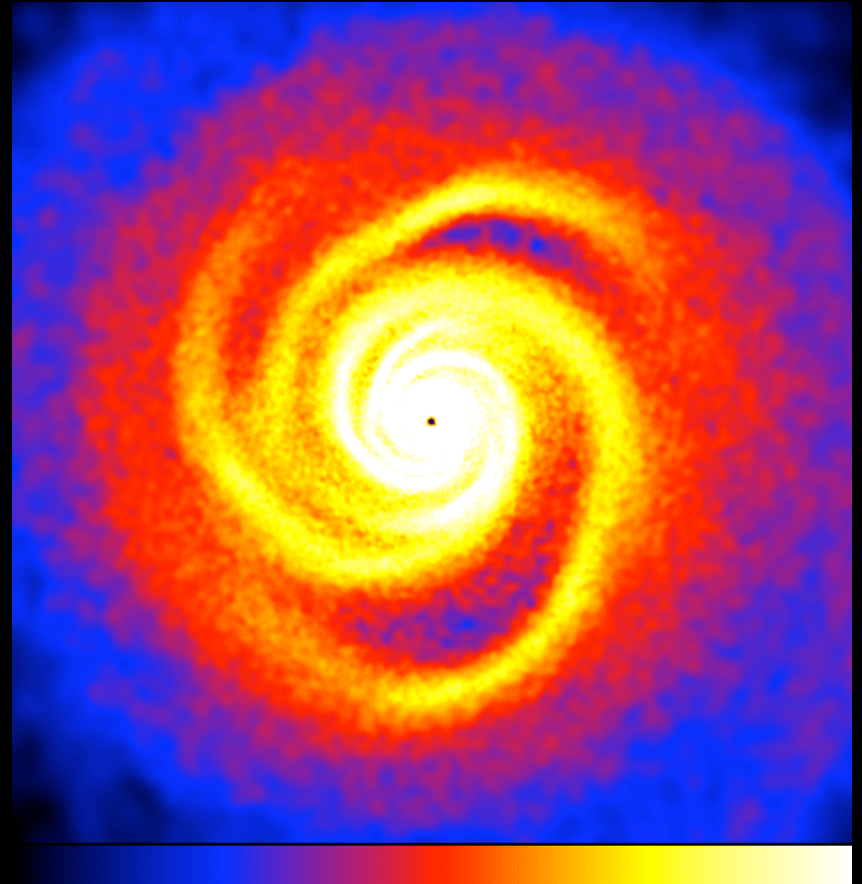
# Growth and migration of a 10 micron-sized particle

(Haghighipour, 2005)



# Self-gravitating discs

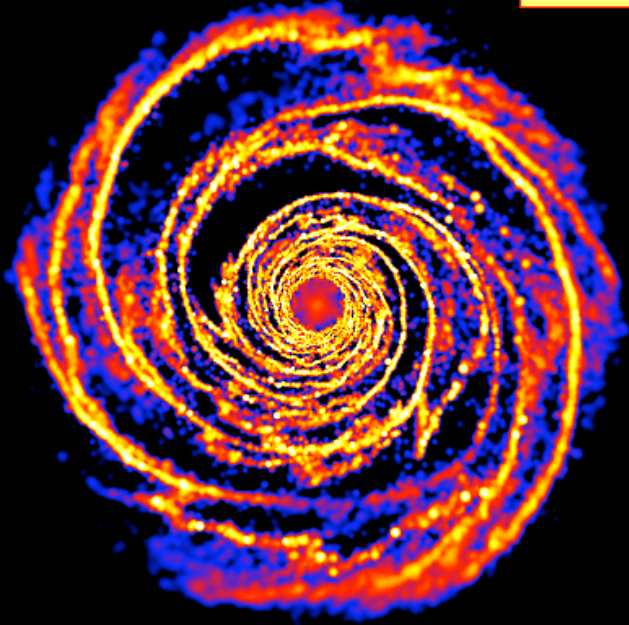
- Pressure gradient changes sign across spiral structures.
- Dust grains/small planetesimals can drift both inwards and outwards.
- Net effect - grains concentrate in the center of the spiral structures (Haghighipour & Boss 2003; Rice et al. 2004).



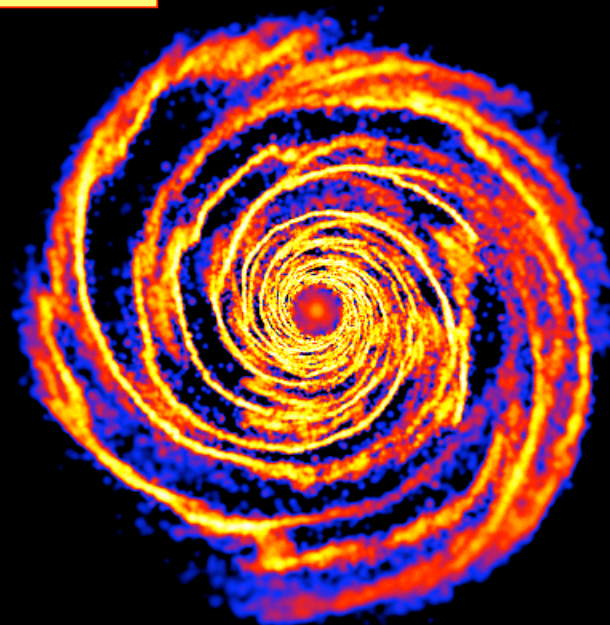


# Direct planetesimal growth

150 cm particles



$$M_{\text{dust}}/M_{\text{gas}} = 1/100$$



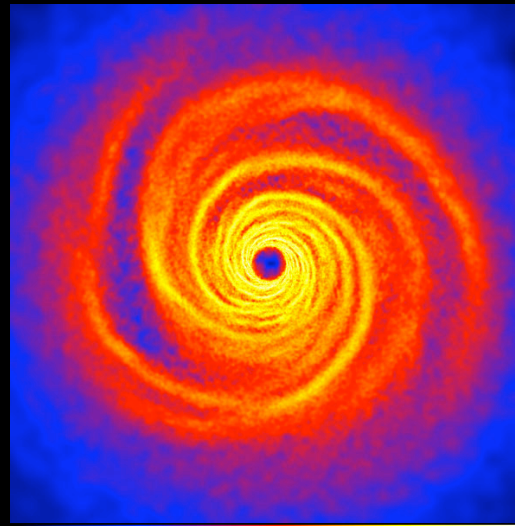
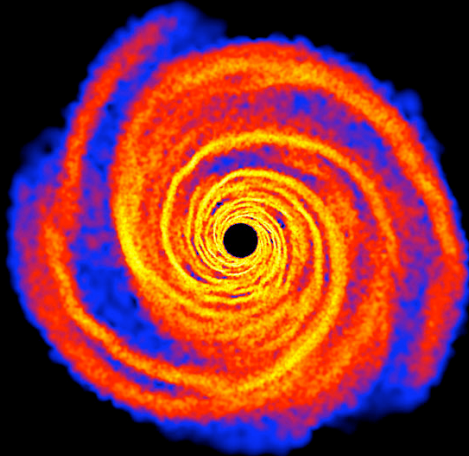
$$M_{\text{dust}}/M_{\text{gas}} = 1/1000$$

- Consistent with the metal-rich nature of planet host stars!

# Dust evolution

- Large particles
  - decoupled from gas.
  - Structure largely matches that of the disc gas.

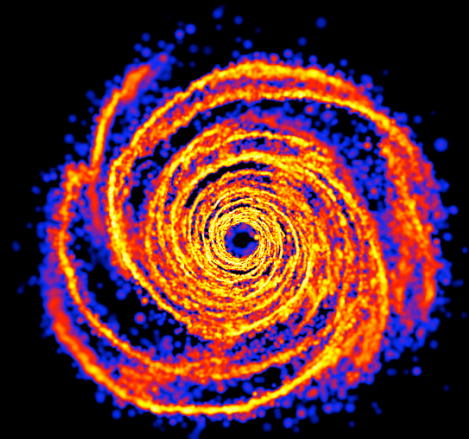
1000 cm



gas

- Intermediate size particles
  - gas drag causes significant drift.
  - concentrate in the center of the spiral arms.

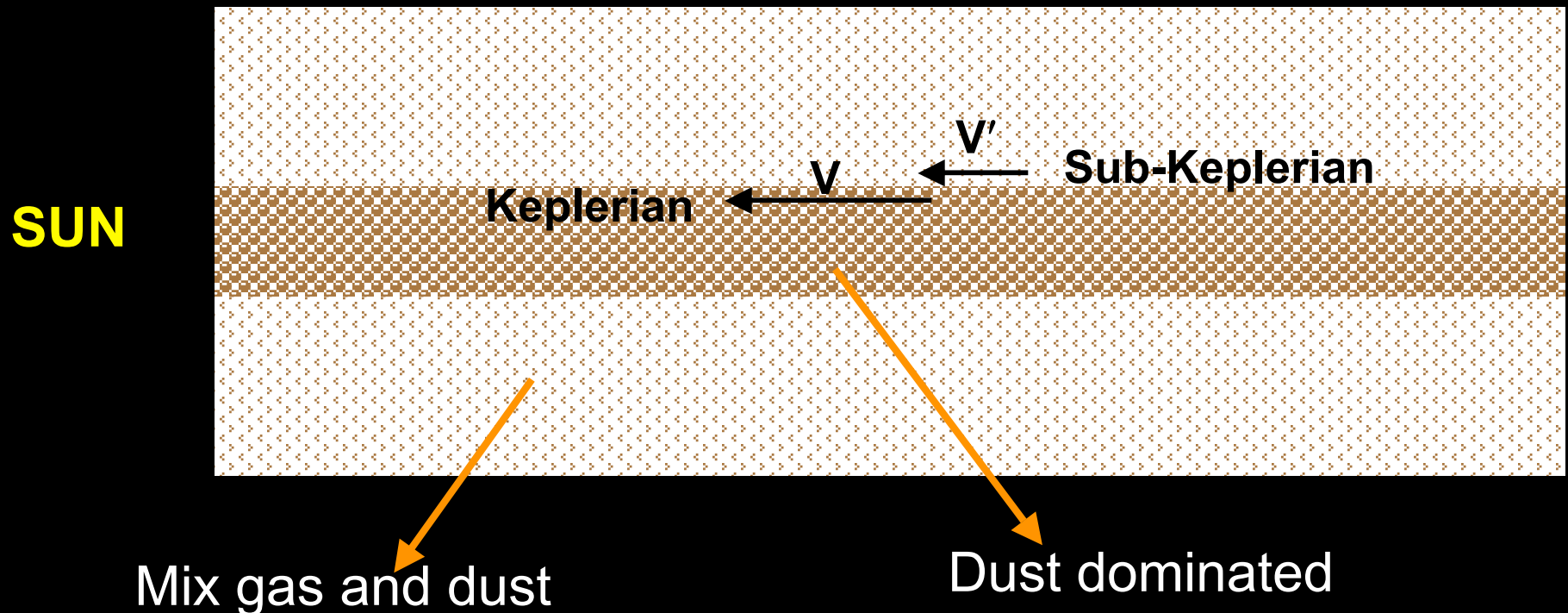
50 cm



(Rice et al. 2004).

# Gravitational Instability

After a dust layer is formed around the midplane, the difference between gas and dust velocities produces Shear-induced turbulence



## Are There Regions in a Nebula where Shear-Induced Turbulence may be Non-existence?

Shear-induced turbulence is caused because there is pressure-gradient.

$$\omega_g = \frac{GM}{(r^2 + z^2)} + \frac{1}{r\rho_g(r,z)} \frac{\partial P_g(r,z)}{\partial r}$$

Are there regions in a nebula where pressure gradient vanishes?

Nebula  $\sim$  Ideal gas

$$P_g = K_B T_g \rho_g / m_H$$



In a region where pressure  
gradient vanishes



$$\frac{\partial P_g(r, z)}{\partial r} \propto \frac{\partial \rho_g(r, z)}{\partial r}$$



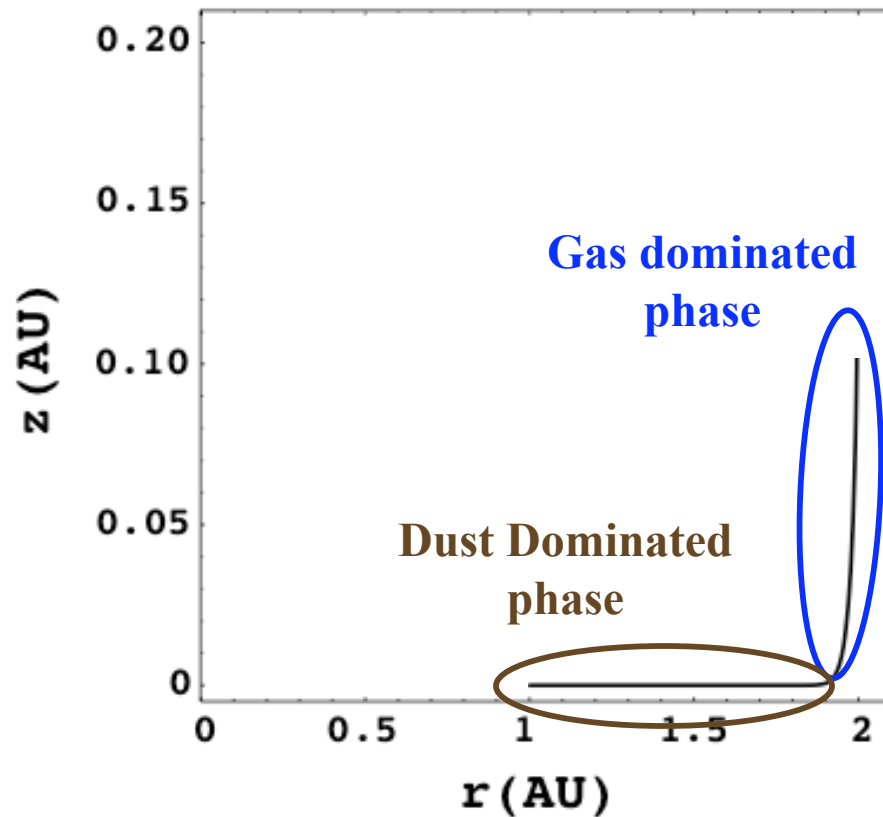
$$\frac{\partial \rho_g(r, z)}{\partial r} = 0$$



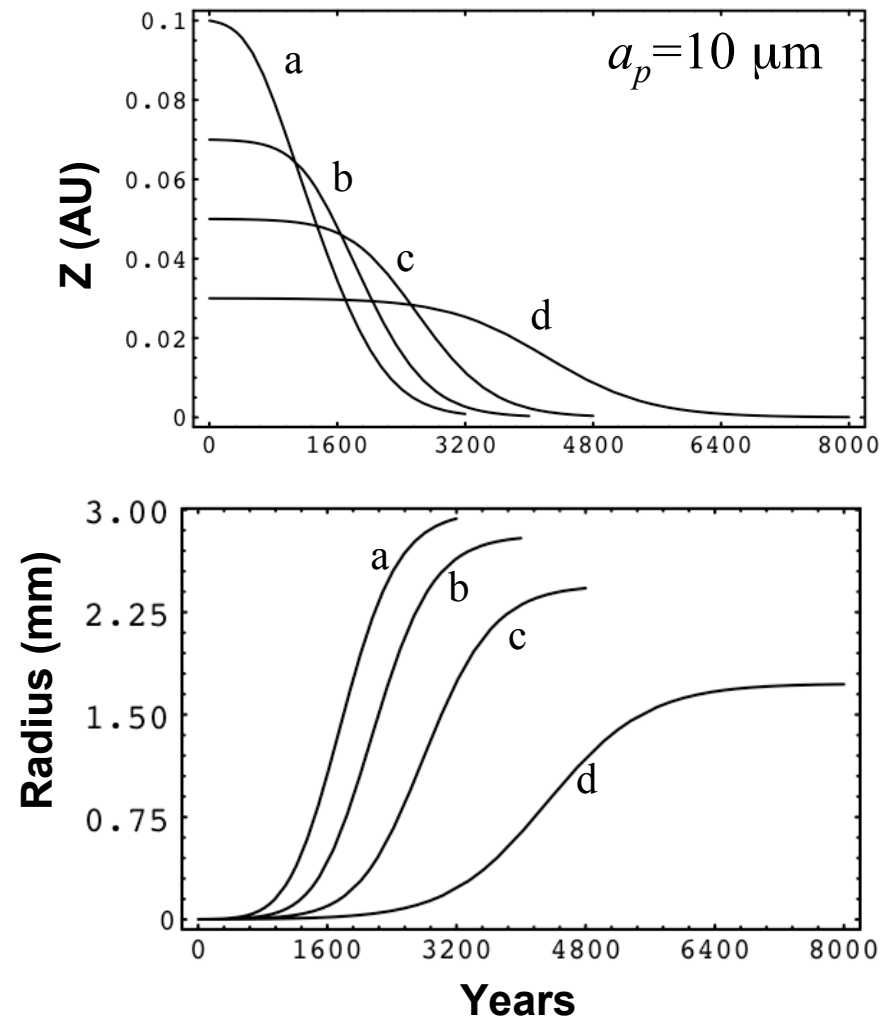
**Regions where the density  
of the gas is maximum are  
shear-induced turbulence-free.**

# Vertical Settling and Particle Growth

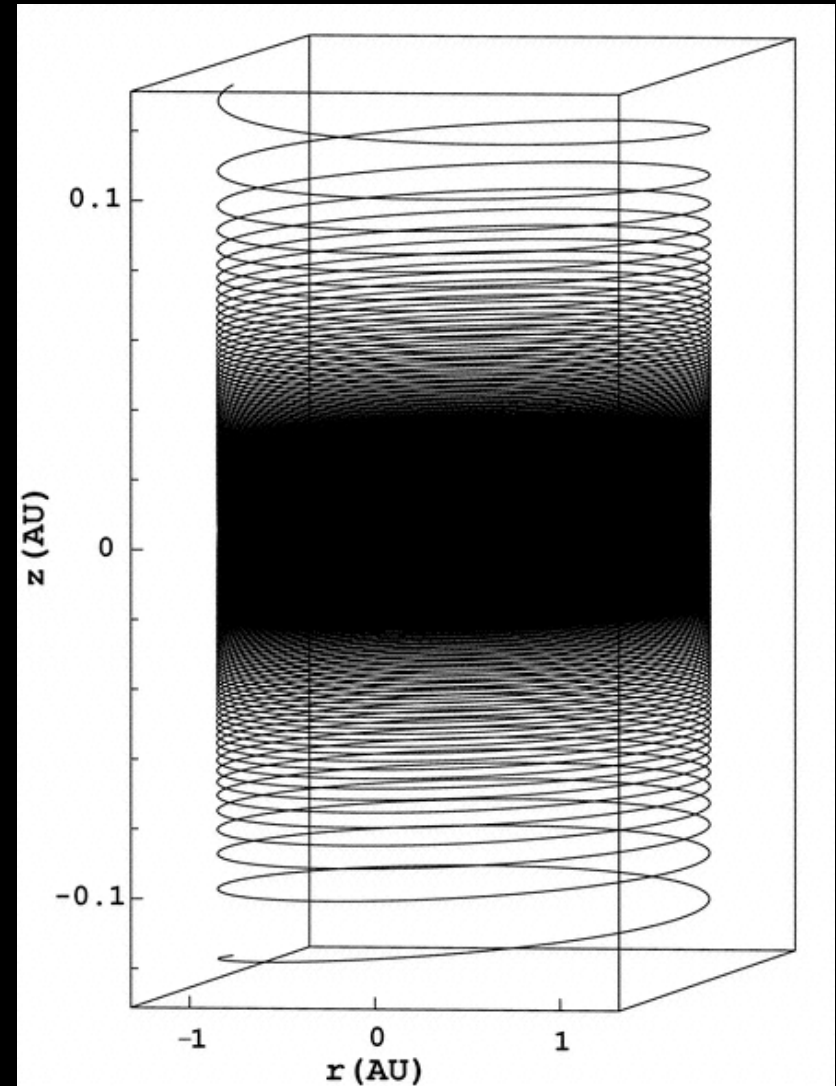
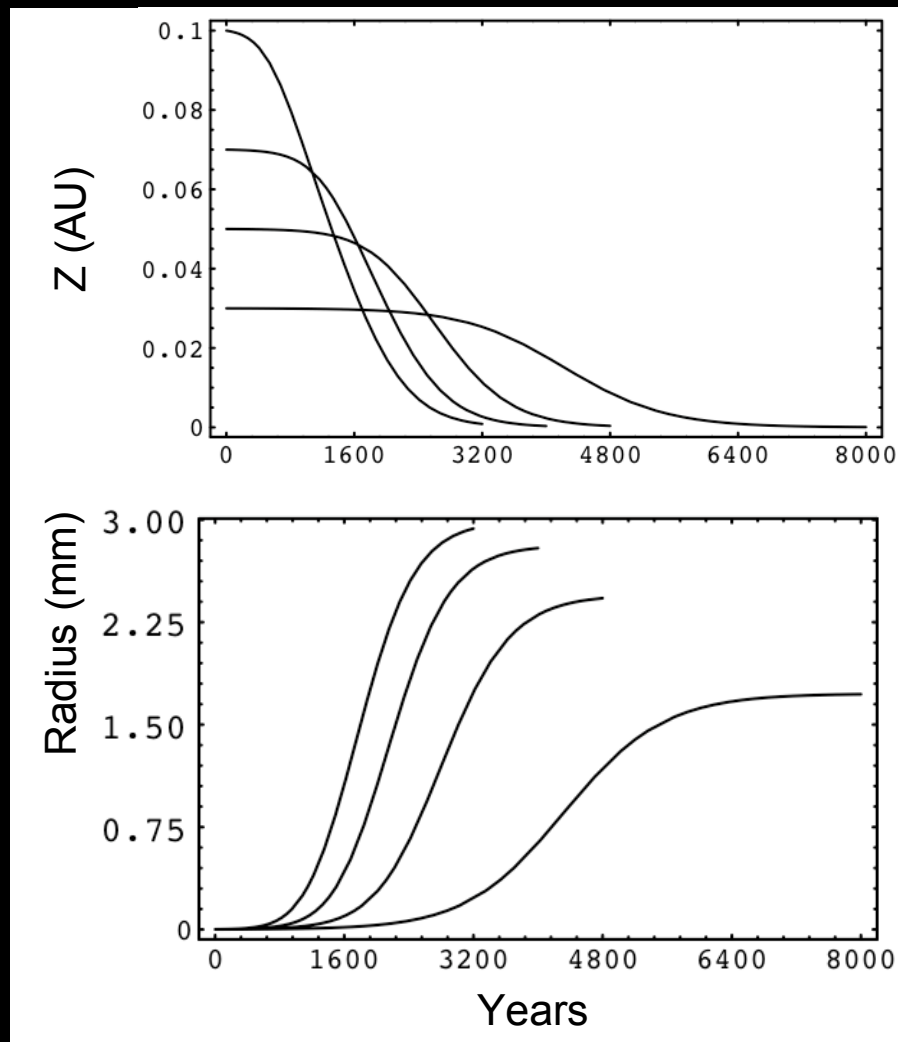
Dust particles grow to mm- and cm-size while settling on the midplane.



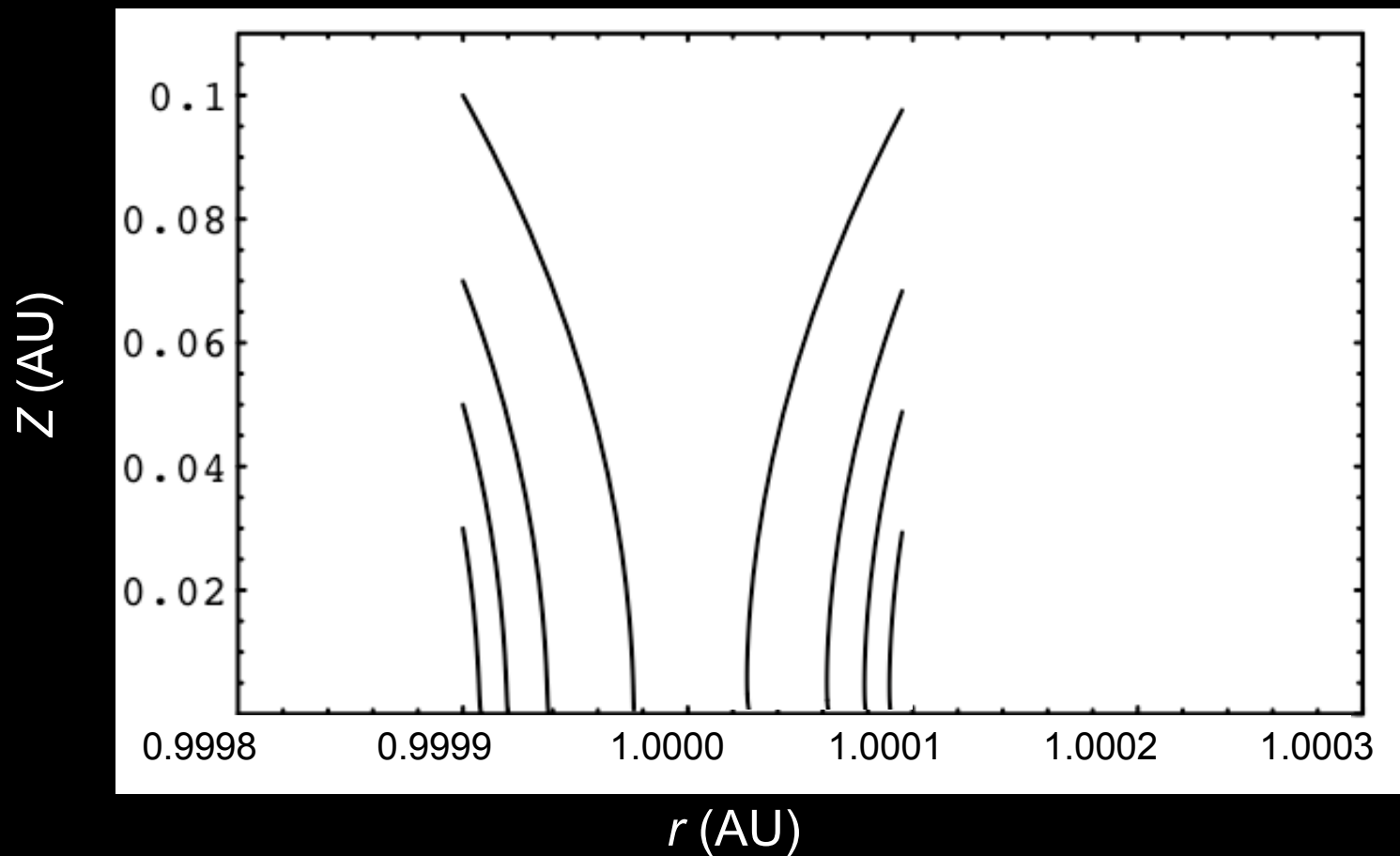
(Haghighipour 2005)



# Growth of a 1 micron-sized particle while descending to the midplane



The midplane at  $r = 1$  (AU) is populated by mm-sized objects in a few thousand years.





## Conclusions

- Combined effect of gas-drag and pressure-gradients causes micron-sized dust particles to migrate towards gas-density enhanced regions while growing to a few millimeter in size.
- The location of the maximum gas pressure/density is turbulence-free since pressure gradients vanish in such locations and the dust and gas rotate at Keplerian velocity.
- Settling dust particles in the location of maximum gas pressure/density form a layer of mm-sized objects which may undergo gravitational instability.
- The appearing and disappearing of gas- density enhanced regions causes the accumulated cm-sized particles to undergo additional migration, and form larger (meter-sized) accumulations.